

# Spectral Line Broadening

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# Natural Broadening

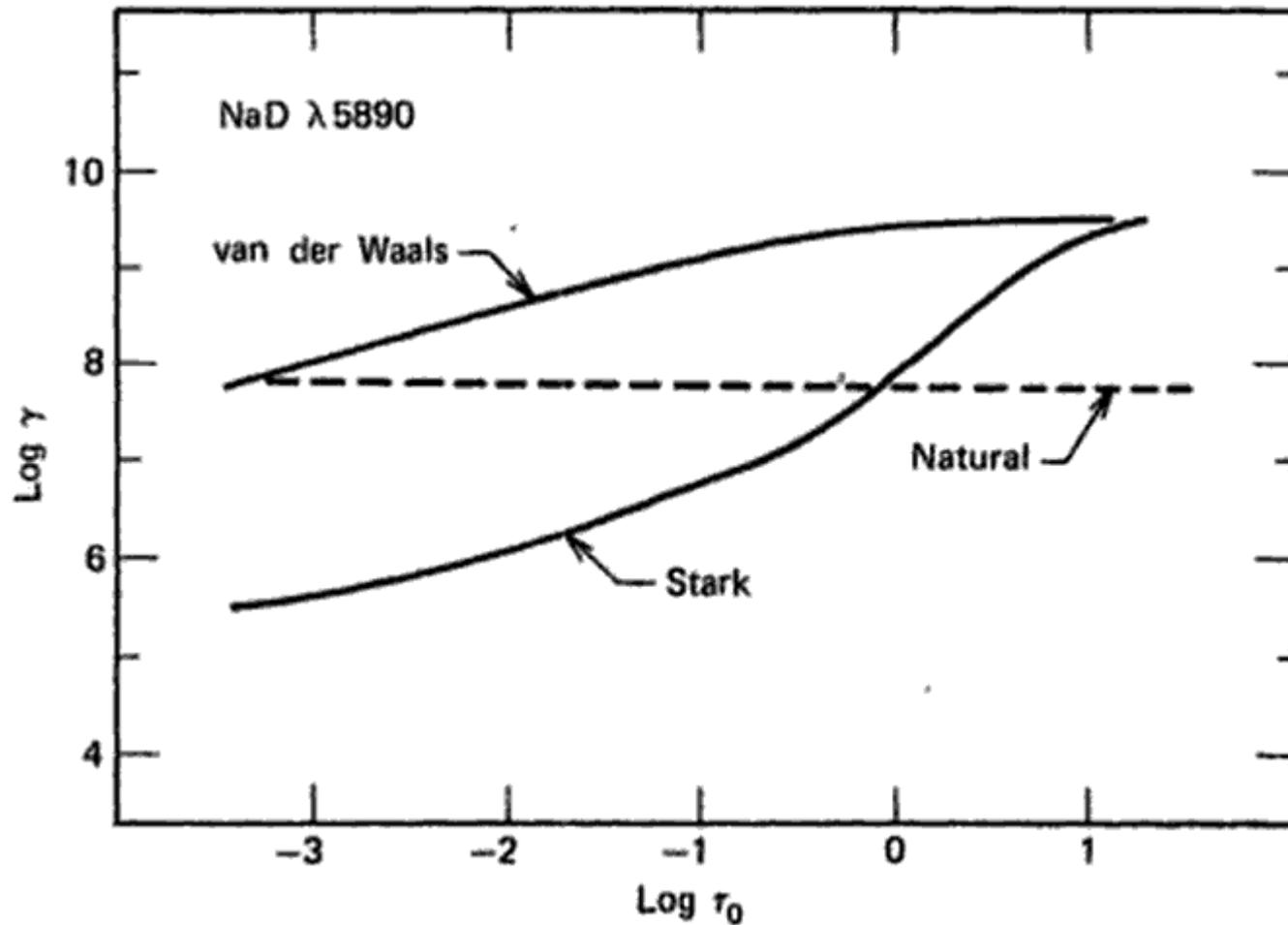
- Uncertainty of energy levels
- Usually much smaller than other broadening mechanisms.
- **Resonance lines**
  - Transition from ground state to first energy level
    - Often the strongest lines
      - Least energy needed

# Pressure Broadening

- Collisional interactions between absorber and other particles
- Perturbs energy level:  $\Delta E \propto r^{-n}$ 
  - Upper level perturbed the most

n	Name	Type	Perturber	Lines affected
2	Linear Stark	H + charged particle	Proton, electron	Hydrogen
3	Resonance	Atom A + atom A	self	Hydrogen
4	Quadratic Stark	Ion + charged particle	electrons	Most lines, esp. hot stars
6	Van der Waals	Atom A + atom B	Usually hydrogen	Most lines, esp. cool stars

# Damping Constants



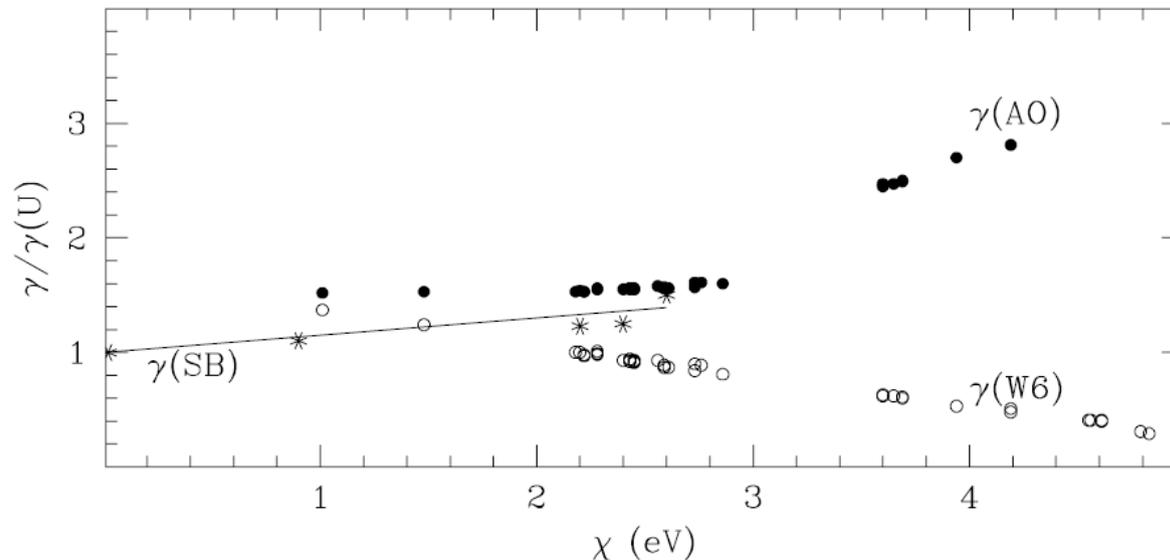
Sodium line for Solar model. [From Gray 1992oasp.book....G](#)

# Damping Constants

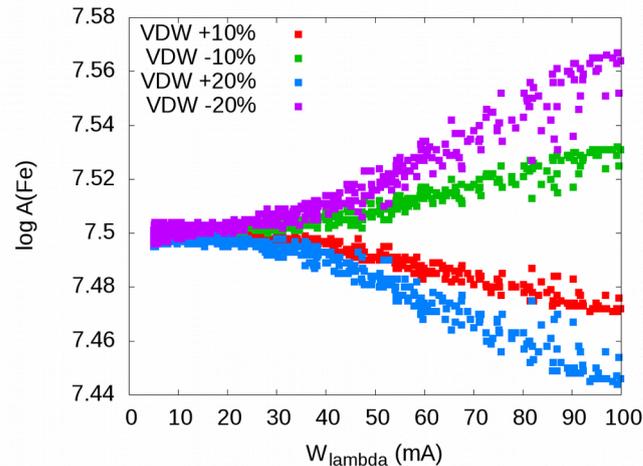
- Lorentz (damping) profile
- Values given in line lists (e.g. VALD)
- What are their accuracies?
  - Some transition probabilities (gf values) have an accuracy (e.g. NIST)
  - Paul Barklem's review 2016A&ARv..24....9B  
*Accurate abundance analysis of late-type stars: advances in atomic physics*

# Collisional Broadening

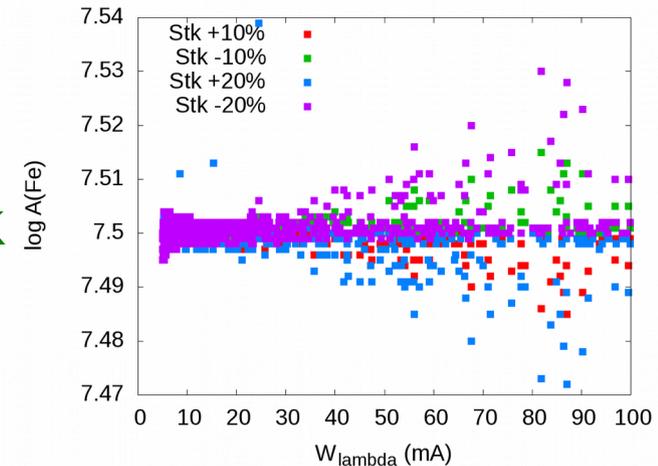
- Ryan 1998 ([A&A, 331, 1051](#))
  - Even weak lines can be affected by damping
  - Damping errors depend on excitation potential
    - errors in microturbulence and effective temperature



# Effect of damping



$T_{\text{eff}}$  6000 K  
Log g 4.5

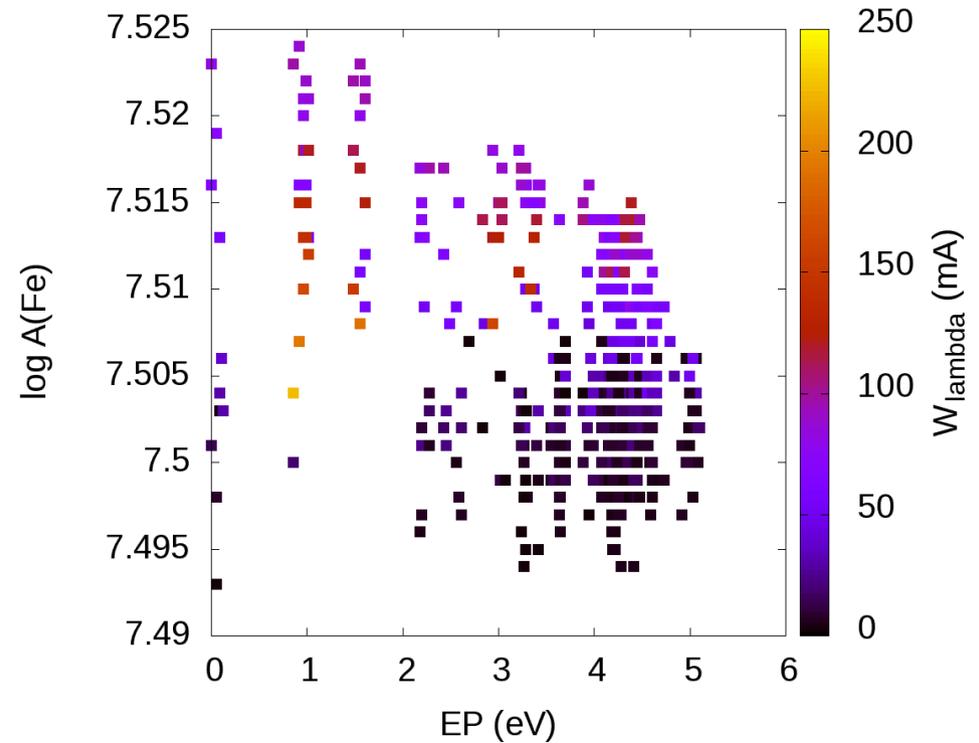
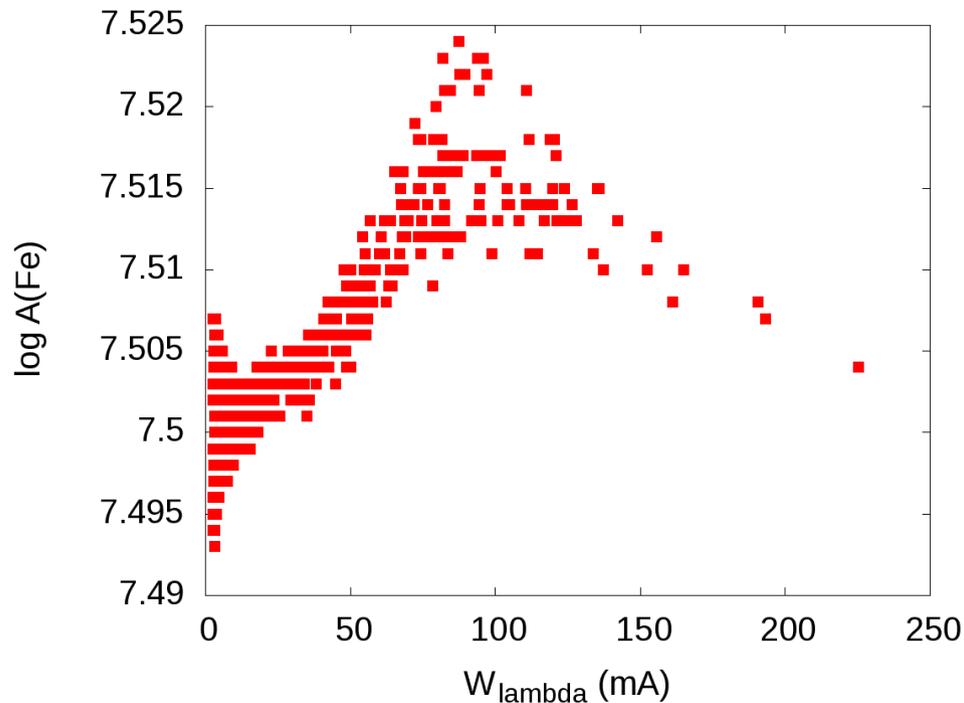


- Errors in damping constants
  - van der Waals (left) and Stark (right)
- VDW could lead to errors in microturbulence

# Astrophysical gf values

- Pros:
  - For Sun well known parameters
  - Differential results
    - Improved precision
- Widely-used and can give good results
  - But, values do depend on model and assumed parameters.
- Cons:
  - Usually assumes shift only due to gf values
    - What about damping, microturbulence, etc.?

# Astrophysical gf Systematics



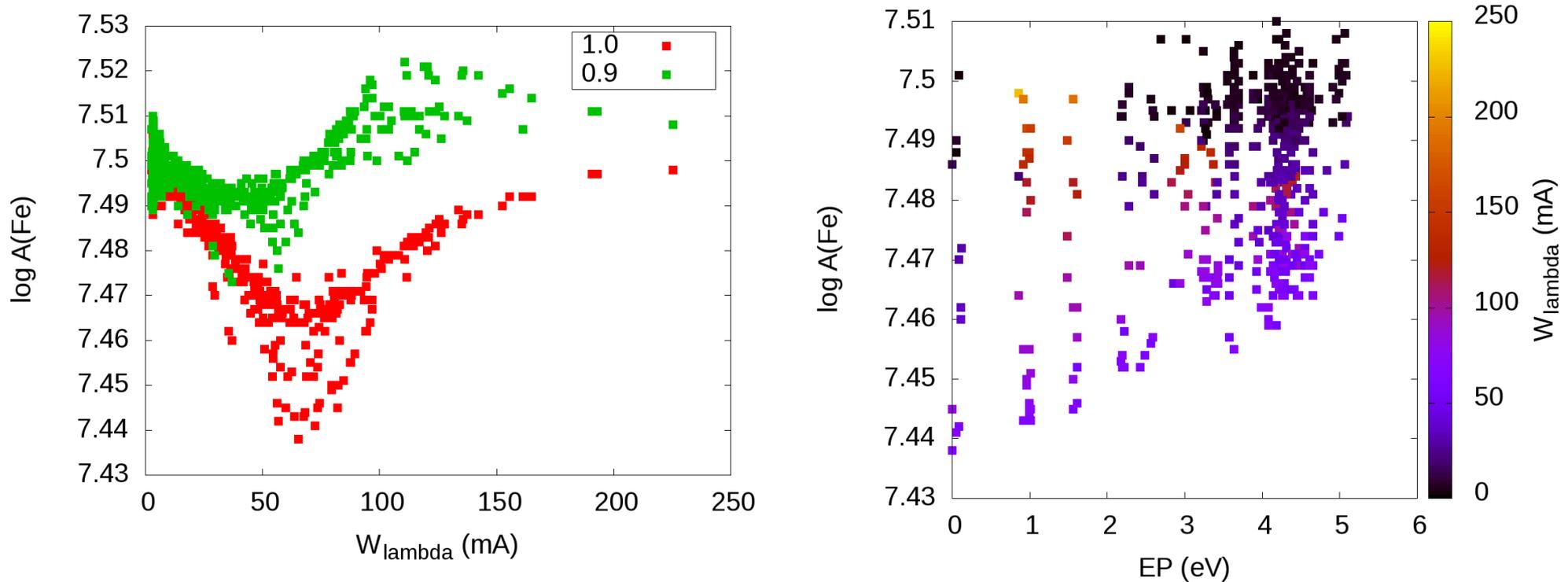
- Astrophysical gf values created at 6000 K but with +20% error in van der Waals damping.
  - Plots show difference in at 6500 K.

# Solar Microturbulence Value

- Edvardsson et al. 1993 ([A&A, 275, 101](#)) 1.15 km/s
- Bruntt et al. 2010 0.95 km/s
- Valenti & Fischer 2005 0.85 km/s
- Santos et al. 2004, ([A&A, 415, 1153](#)) 1.00 km/s
- Magain (1984) 0.85 km/s (centre of solar disk)
  - From Blackwell et al. 1984, ([A&A,132, 236](#)) using Holweger & Mueller 1974, ([SoPh, 39, 19](#)) Solar model

Which to use in Astrophysical gf determination?

# Astrophysical gf Systematics

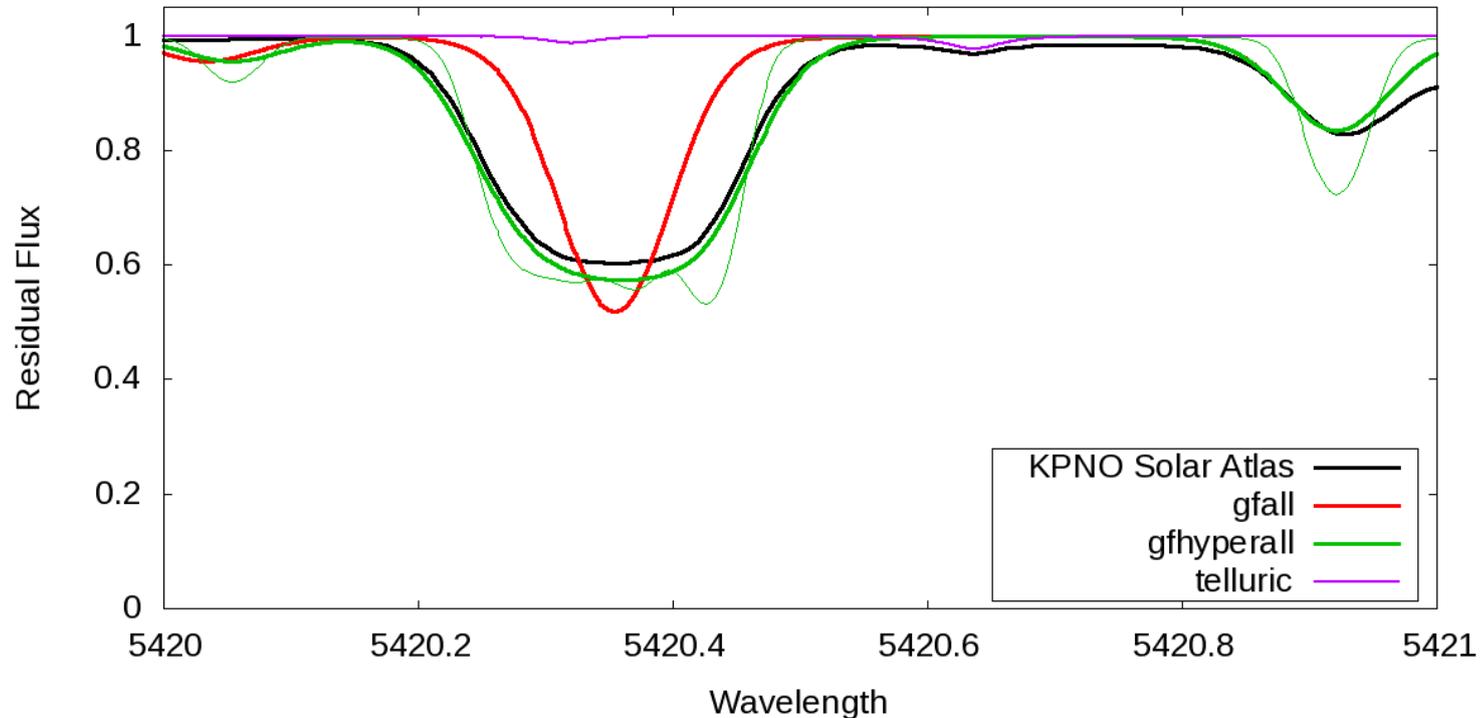


- Astrophysical gf values created at 6000 K but with assumed microturbulence too low by 0.1 km/s.
  - 0.9 km/s instead of “*true*” 1.0 km/s
- Plots show difference at 6500 K

# Zeeman and Hyperfine Splitting

- Zeeman
  - Splitting of energy levels due to magnetic field
- Hyperfine
  - Intrinsic due to nuclear structure
- Isotopes
  - Most line lists assume solar isotopic mix.

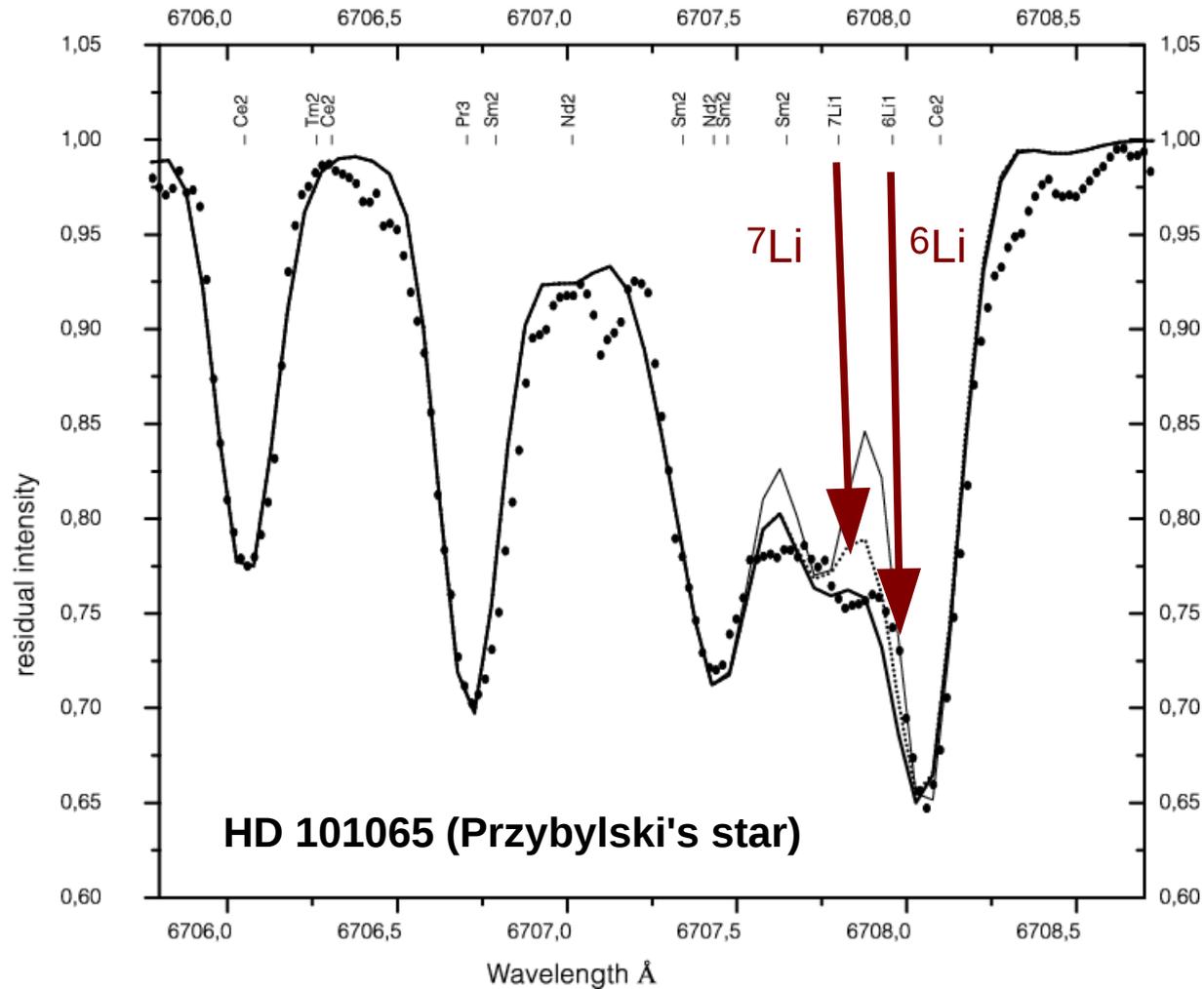
# Hyperfine Structure



Solar Mn I  
line at 5420Å

- The splitting of energy levels in odd atomic elements
  - Multiple components to spectral lines
    - See Wahlgren, 2005, MSAIS, 8, 108

# Non-solar Lithium isotopic ratio

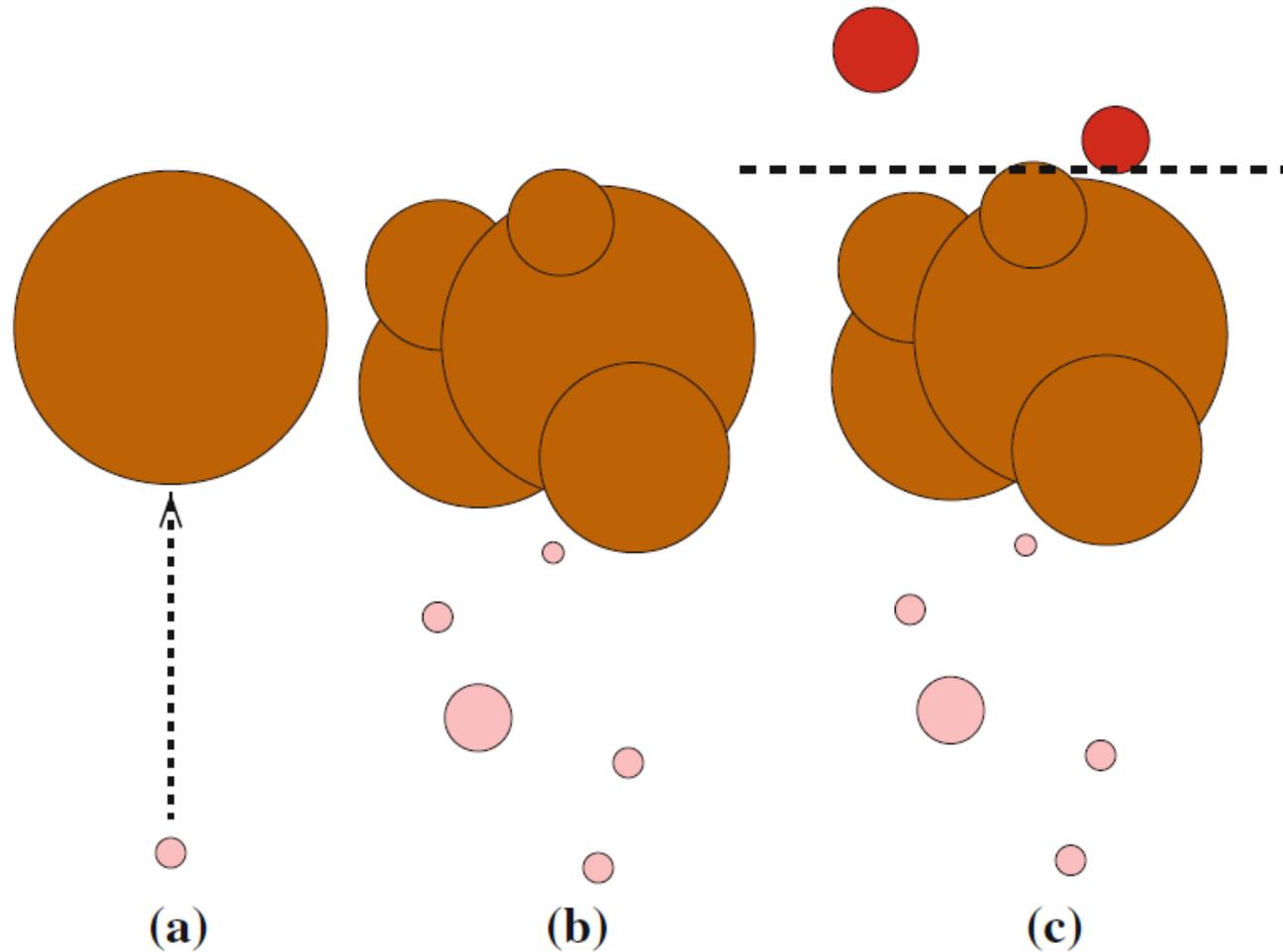


2003A&A...409..707S

# Convection and turbulence

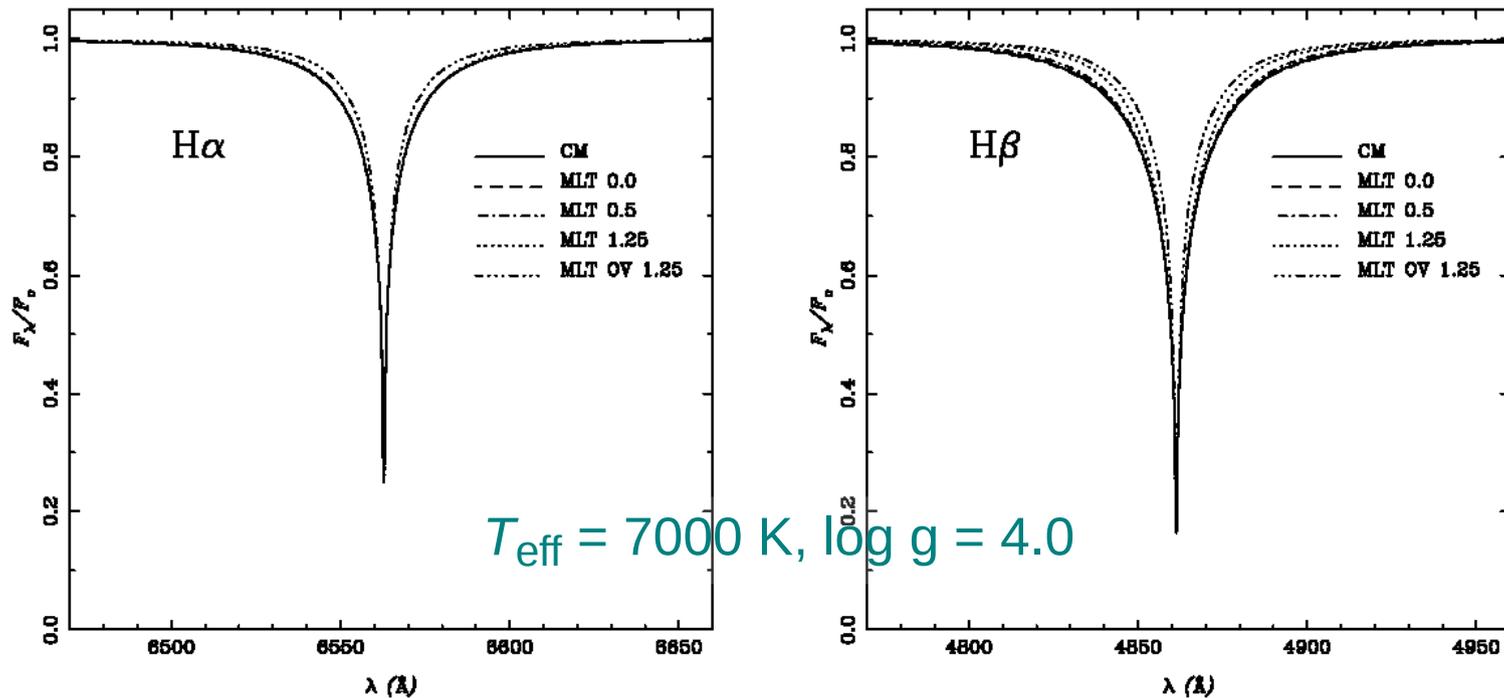
- Effects the atmosphere of A stars and cooler.
- Visible as Solar Granulation
  - Surface convection cells
- Indirectly inferred via
  - Microturbulence
  - Macroturbulence
  - Line bisector curvatures
- Free parameters in 1-d models
  - Can vary with depth in atmosphere

# Convection Models



**Fig. 1** Schematic bubble representations of convection treatments. In mixing-length theory (a), a single bubble rises within the atmosphere, while in turbulent convection bubbles of varying sizes rise (b). In (c) we have overshooting above the convection zone

# Balmer profile variations



- Formed at different depths within atmosphere
  - probe differing parts of atmospheric structure
- Changing the efficiency of convection, by increasing mixing length, has significant effect on computed profile

# Balmer profile sensitivities

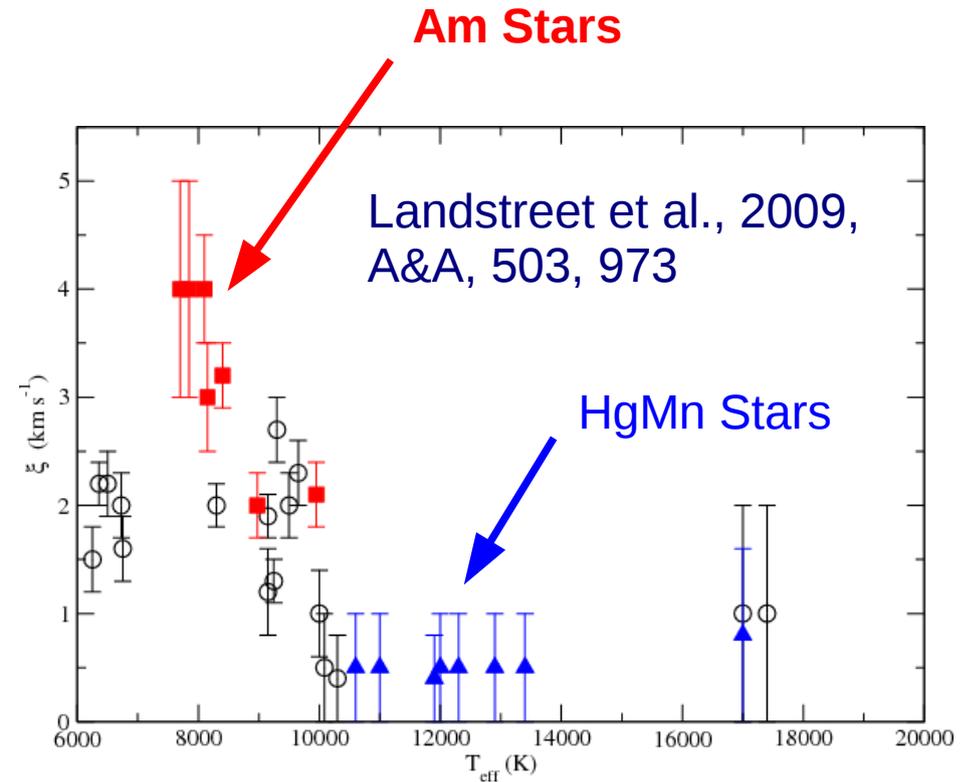
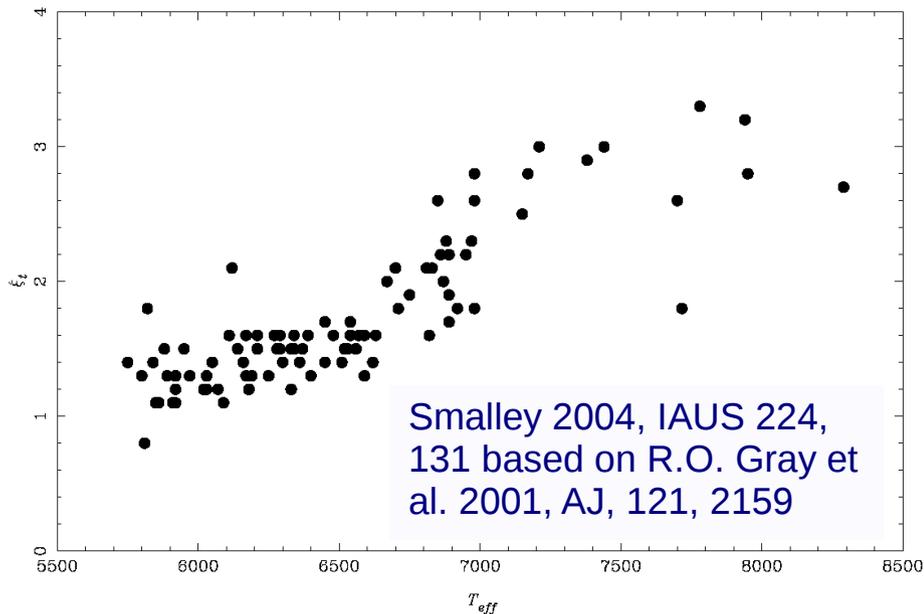
- $H\alpha$  insensitive to mixing-length
- $H\beta$  sensitive to mixing-length
- Both lines affected by overshooting
  - sensitive to temperature and metallicity
  - surface gravity sensitivity for hotter stars

Van't Veer & Megessier, 1996, A&A 309, 879

# Microturbulence

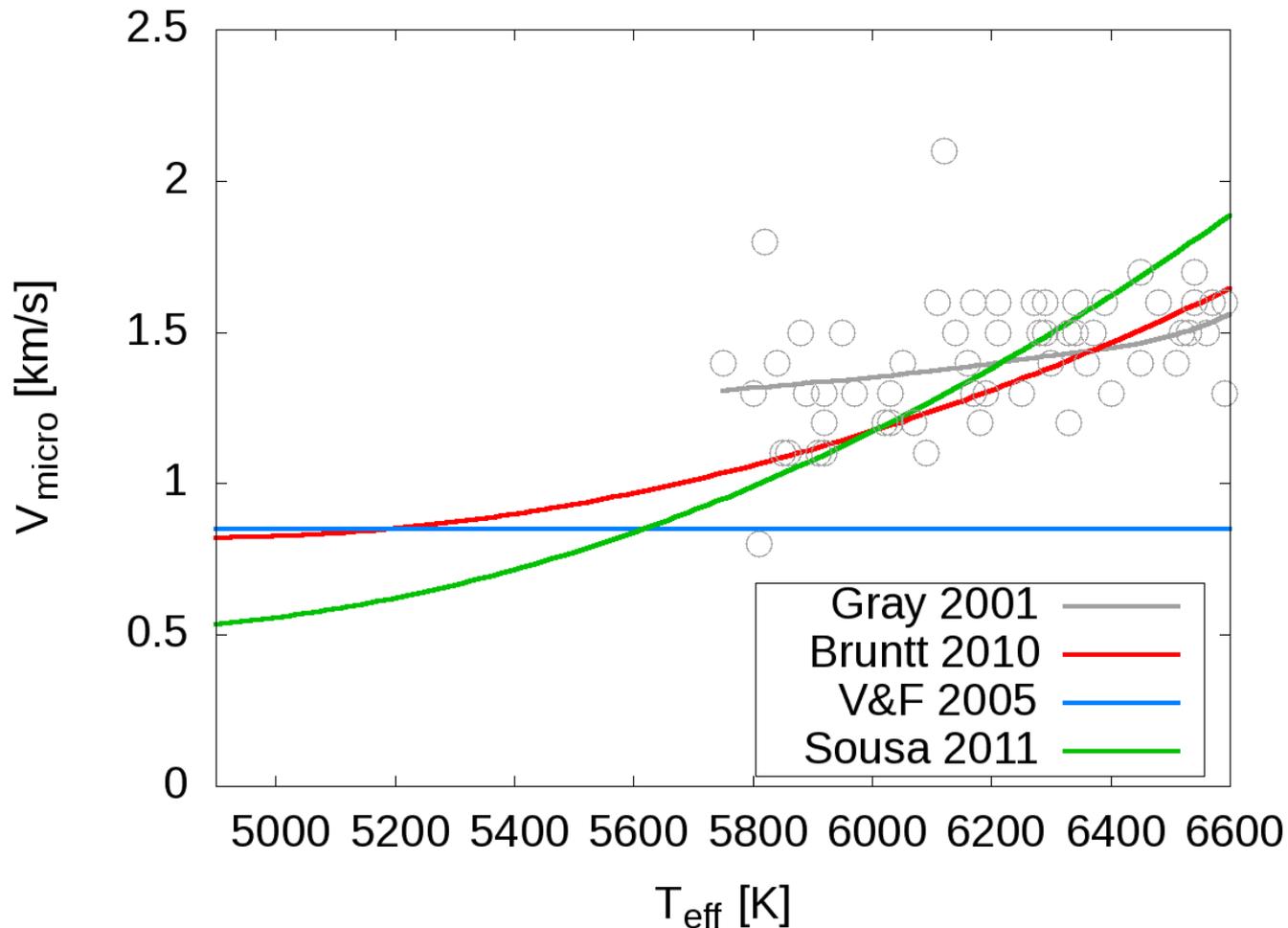
- A **free** parameter introduced to ensure that abundances from weak and strong lines agree
- Extra source of broadening
  - added to thermal broadening
- Small scale motions within the atmosphere

# Microturbulence Variations



- Microturbulence varies with  $T_{\text{eff}}$ 
  - increases with increasing temperature
    - peaking around mid-A type

# Microturbulence Calibrations

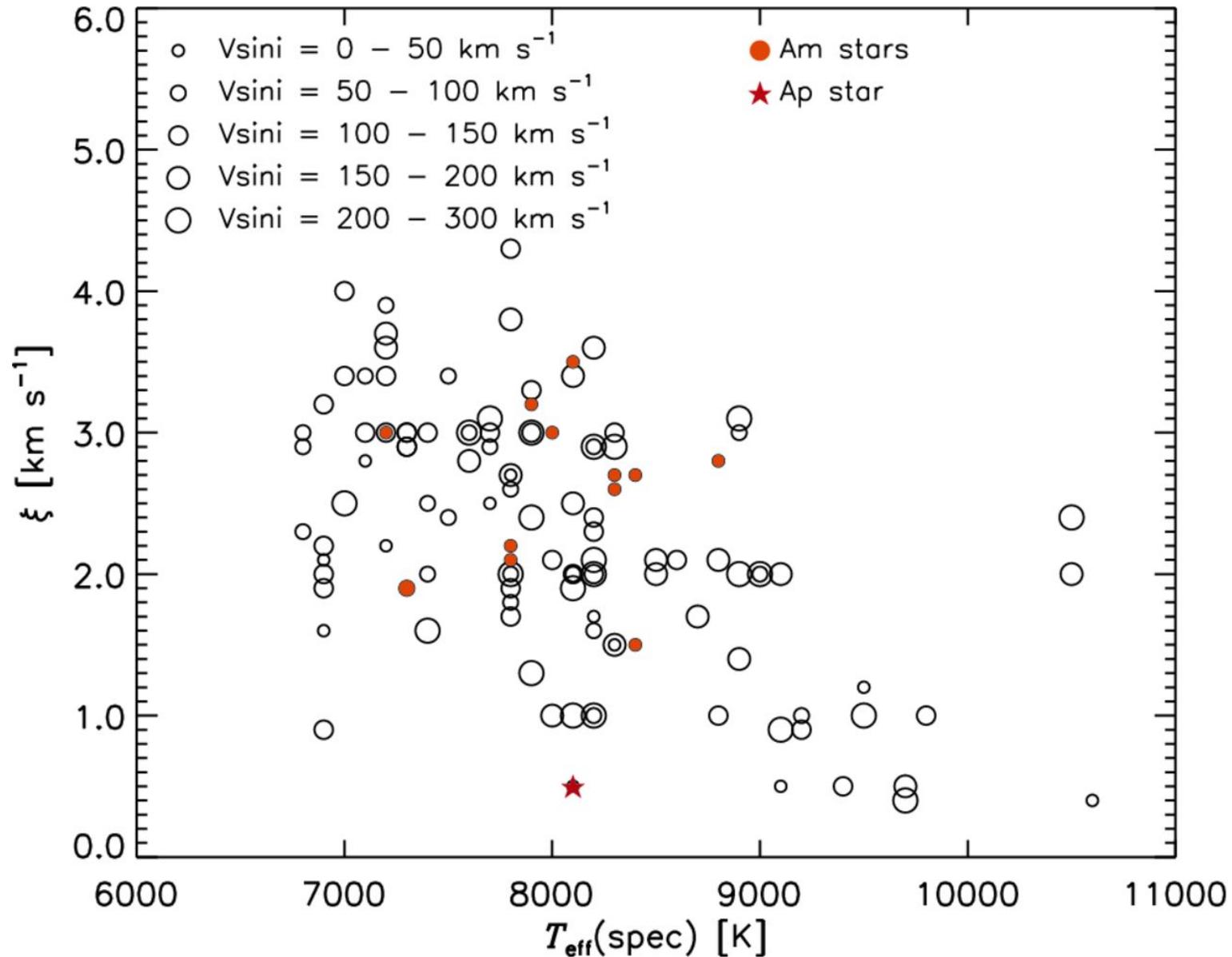


Valenti & Fischer 2005 found: “strongly correlated values of  $v_{\text{mic}}$  and  $[M/H]$ , suggesting that  $v_{\text{mic}}$  and  $[M/H]$  are partially degenerate.” Adopted fixed value.

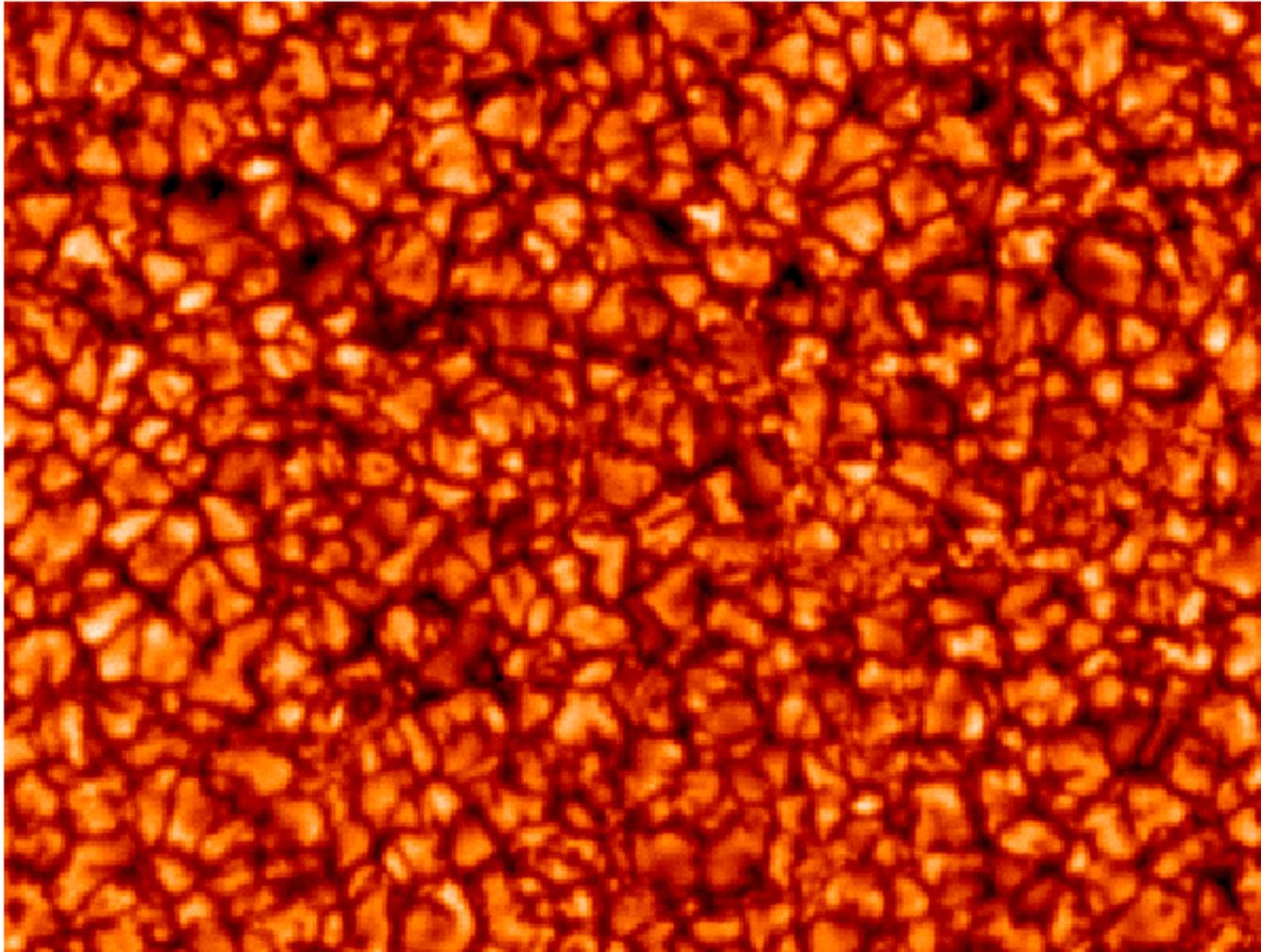
Gray 2001 fit by Smalley 2004 IAUS 224, 131  
Sousa 2011 is fit given in 2013ApJ...768...79G

Valenti & Fischer, 2005, ApJS, 159, 141  
Bruntt et al., 2010, MNRAS, 405, 1907

# Microturbulence in A and B stars



# Solar Granulation

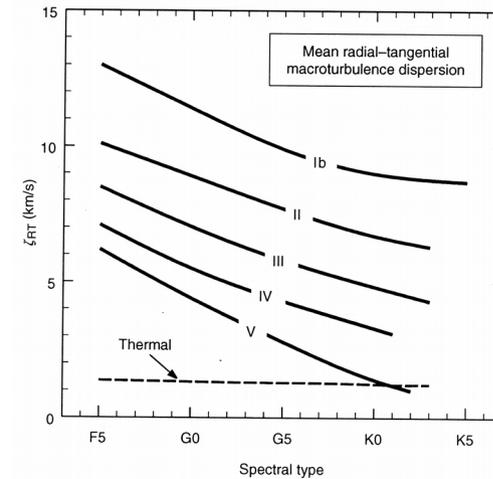
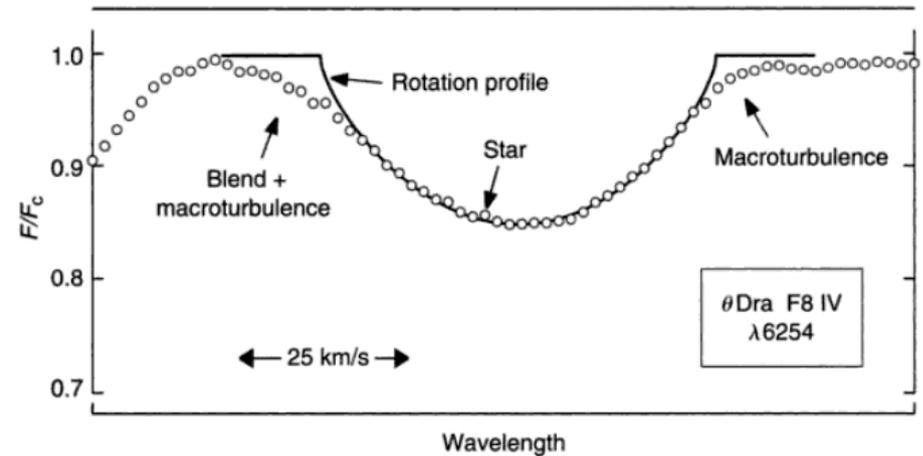


[http://zeus.nascom.nasa.gov/~dmueller/gran\\_intro.htm](http://zeus.nascom.nasa.gov/~dmueller/gran_intro.htm)

# Macroturbulence

- Extended shallow wings
- Strong in giants and supergiants
- Seen in A-type stars
- Even B supergiants
- Przybilla et al., 2006, A&A, 445, 1099

**Large-scale velocities  
within atmosphere**



# Gray's Radial-Tangential Model

- Doppler broadening in both radial and tangential directions
  - $\frac{1}{2}$  surface radial
  - $\frac{1}{2}$  surface tangential
- Assume same velocity for both ( $\zeta_{RT}$ )

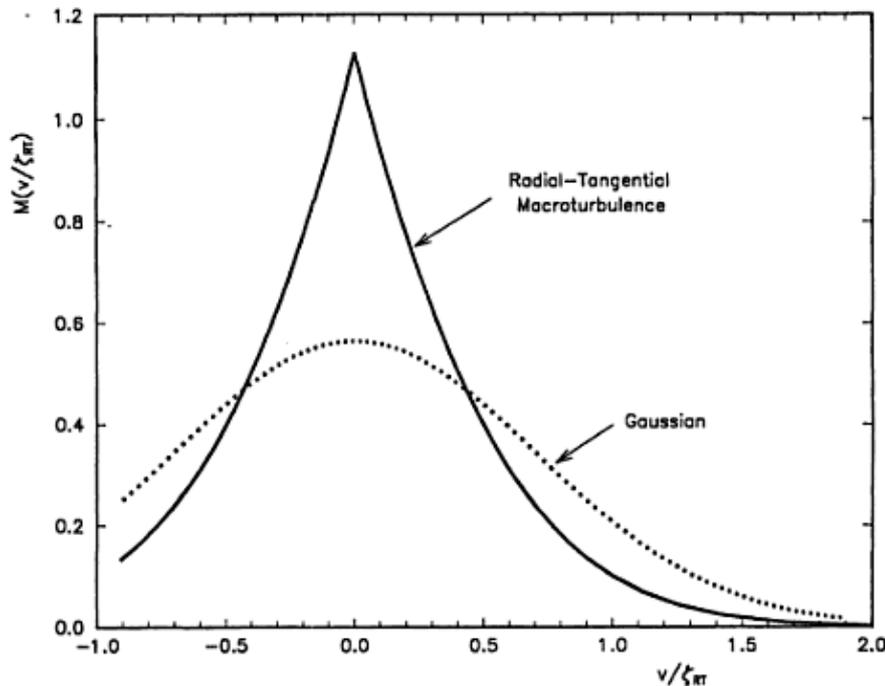
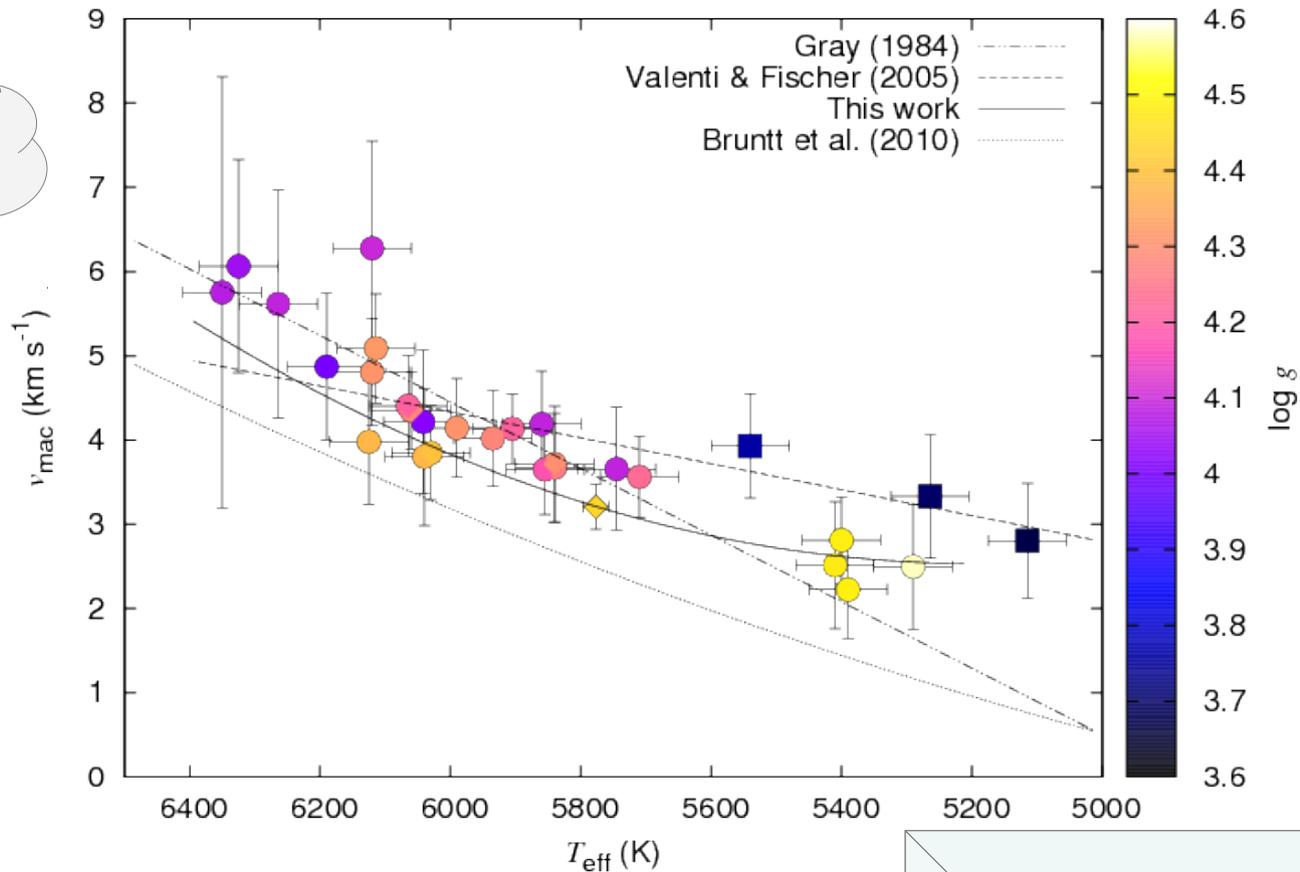


Fig 17.5 D.F. Gray (2008) Book

*A free parameter*

# Macroturbulence in solar-type Stars

Calibration  
for A/F stars?



2014MNRAS.444.3592D

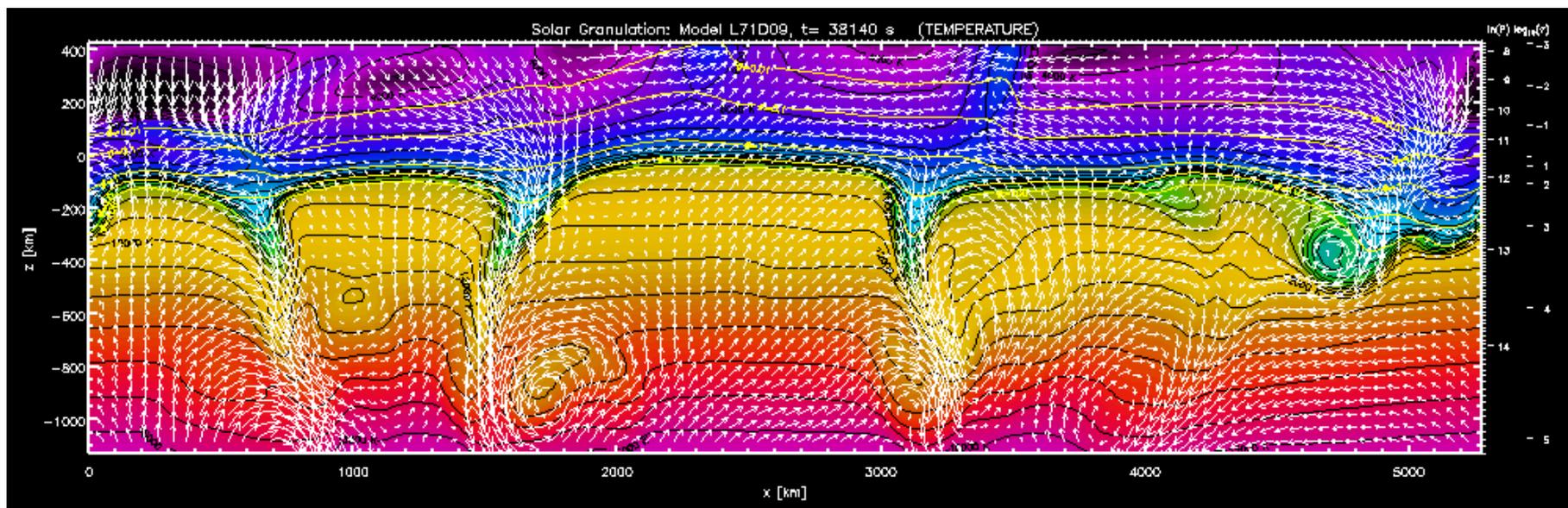


Calibration using  
Kepler asteroseismic  
 $v \sin i$  values

# No need for microturbulence and macro-turbulence

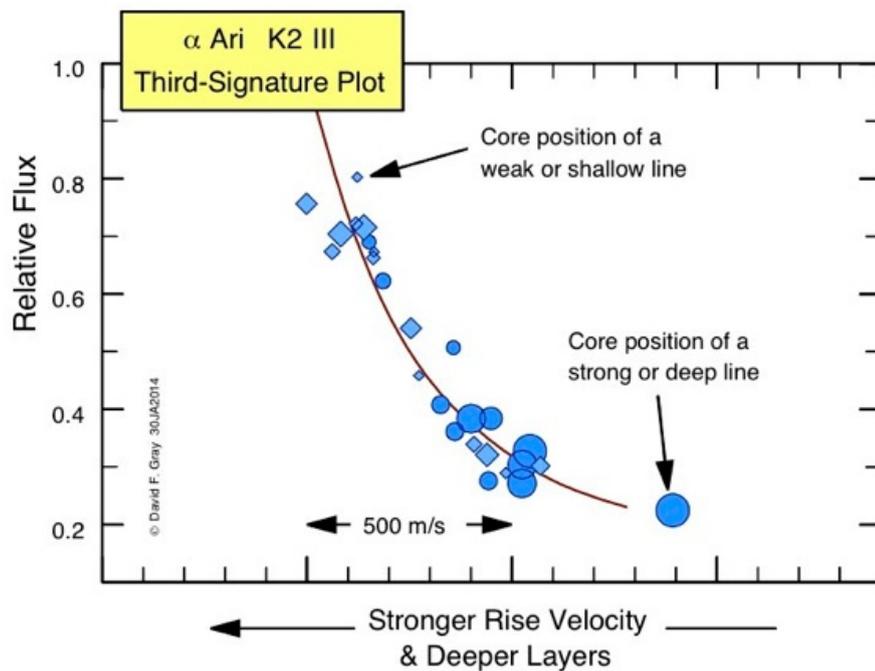
- Numerical simulations avoid the need for such free parameters (e.g. Asplund et al., 2000, A&A 359, 729)
  - not turbulent motions, but velocity gradients

**No longer free parameters and should be constrained when using 1-d models**



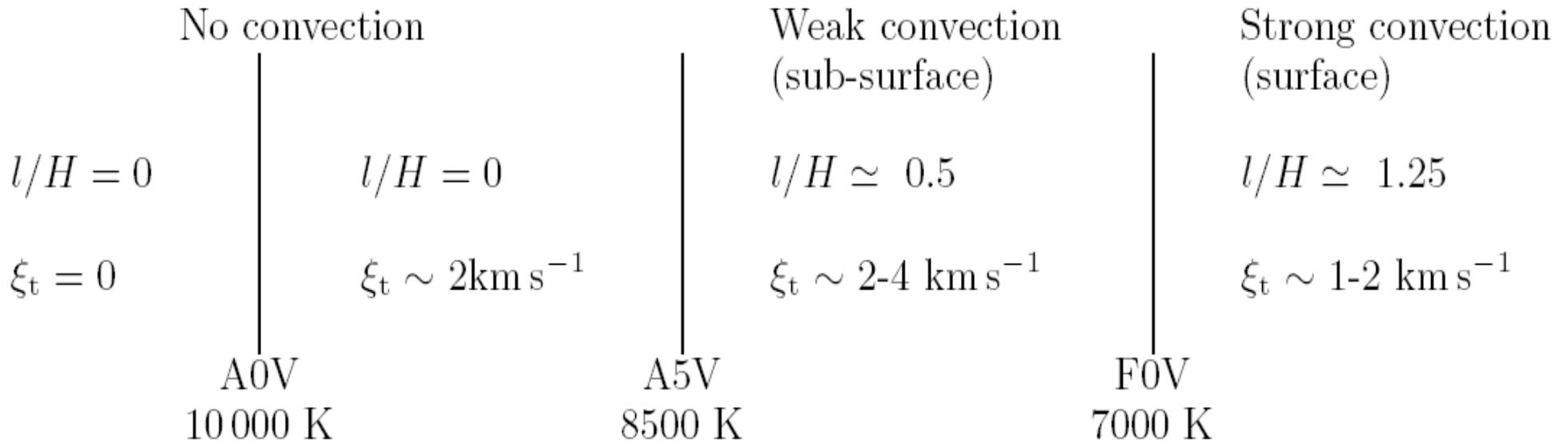
# Spectral Line Shifts

- Position of line cores shifted by velocity fields
  - Vary with depth
  - Time variable
    - “noise” in radial velocity measurements



<http://www.astro.uwo.ca/~dfgray/Granulation.html>

# A Convection Recipe



Smalley, 2004, IAUS 224, 131

# Stellar Rotation

- Doppler shifts due to stellar rotation
- Characteristic broadening shape.
- Normally assume solid-body rotation of a spherical star
- Observe projected rotation velocity ( $v \sin i$ )

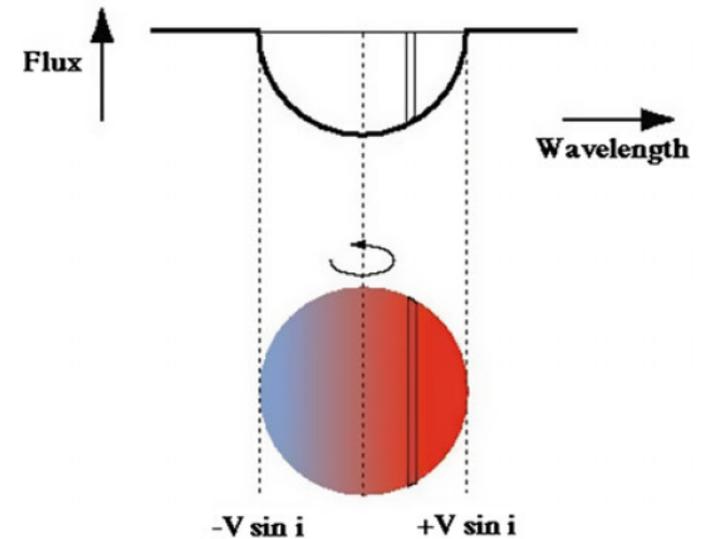
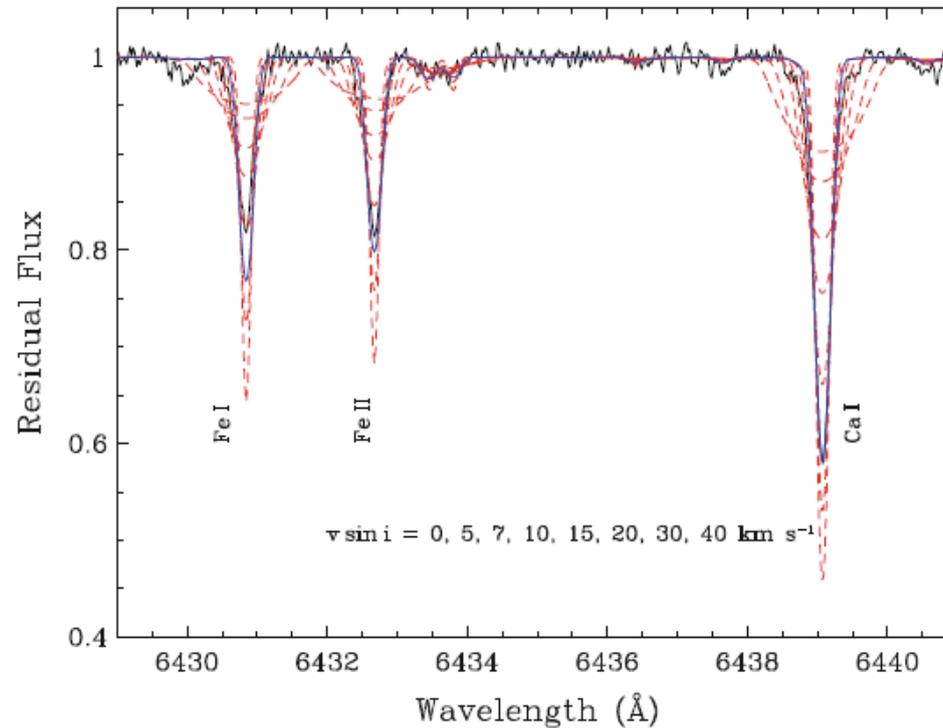


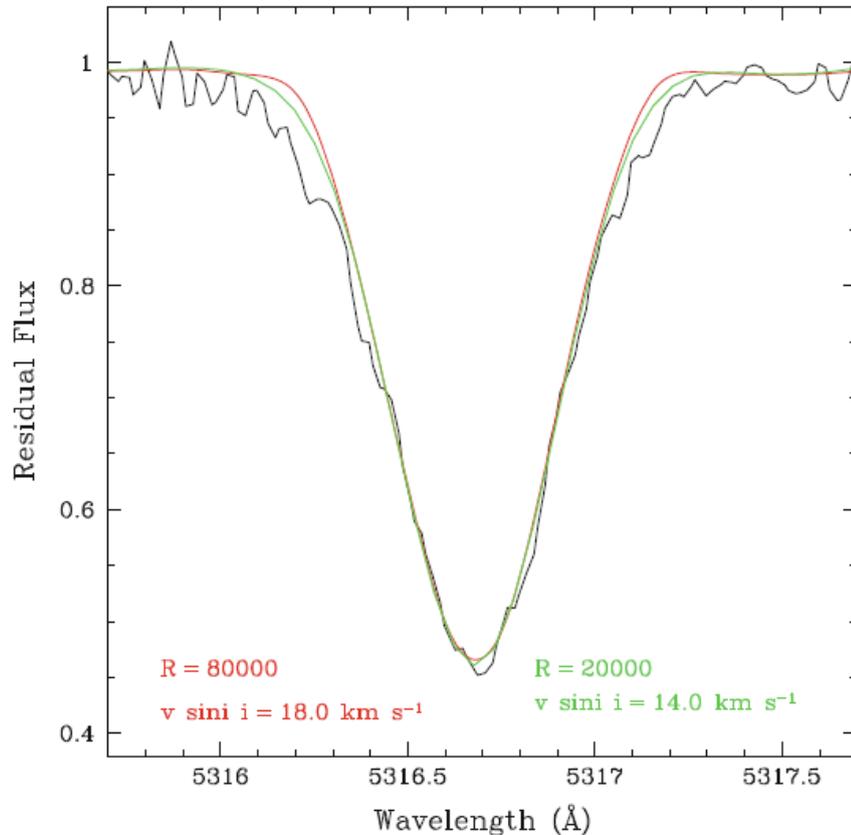
Fig. 1 Schematic view of the Doppler broadening of a spectral line due to rotation

# Determining $v \sin i$



**Fig. 4** Part of an observed spectrum with several synthetic spectra overimposed. Each synthetic spectrum was computed for different value of rotational velocity. The best fit is achieved for  $v \sin i = 7 \text{ km s}^{-1}$

# Effect of Resolution



- Spectrograph resolution can be important.
- Ensure that the correct resolution is used when determining  $v \sin i$ .

2014dapb.book..121C

# Summary

- Some broadening mechanisms are fixed for all stars and come in the linelists used:
  - Damping Constants
    - Natural (Radiative)
    - Pressure (Stark, VDW)
- Other mechanisms depend on the star.
  - Thermal (Doppler) Broadening
  - Microturbulence
  - Macroturbulence
  - Rotation
- Some are (or can be) free parameters
  - even when they ought not to be!